



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



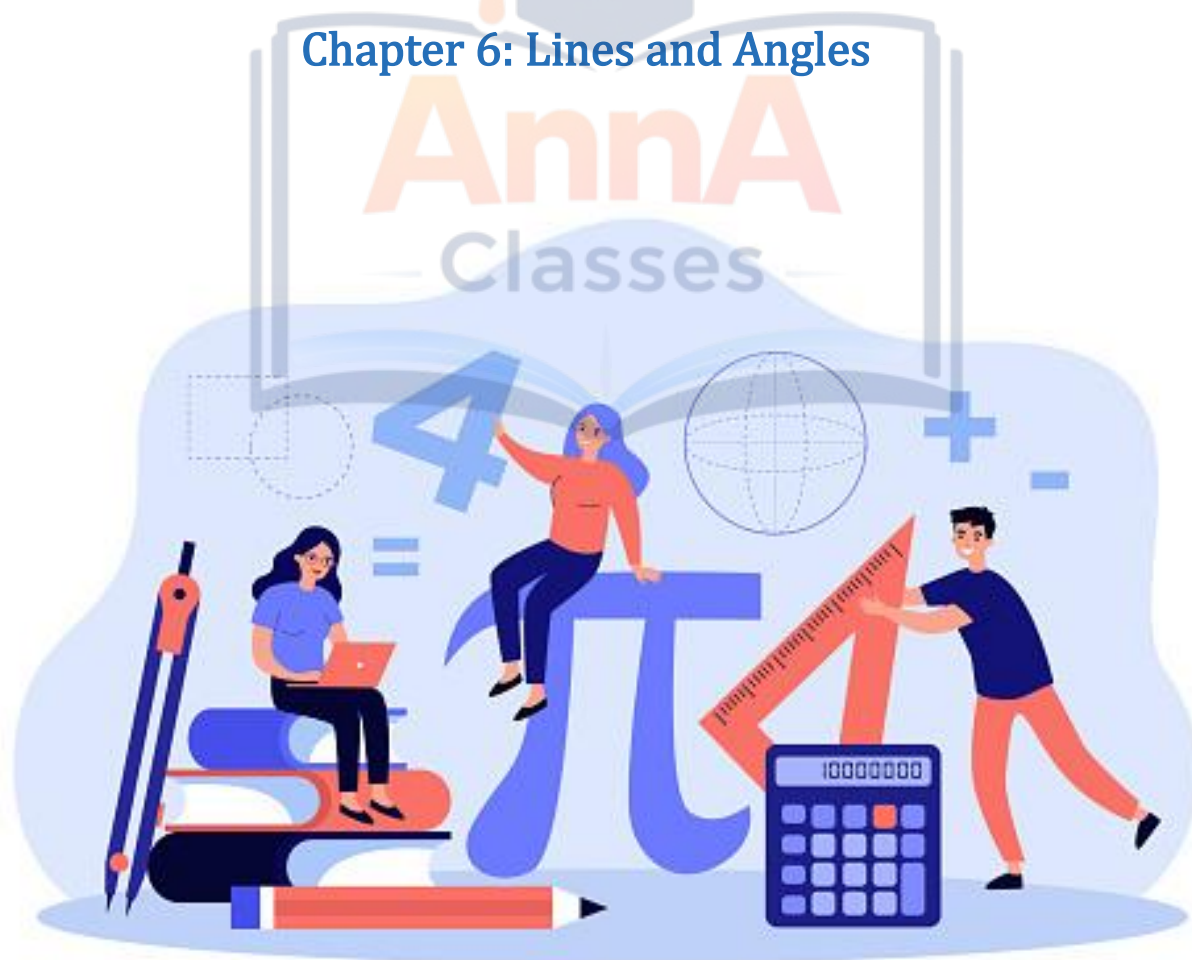
annaclasses.btb@gmail.com



annaclassesonline.com

MATHEMATICS

Chapter 6: Lines and Angles





AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com

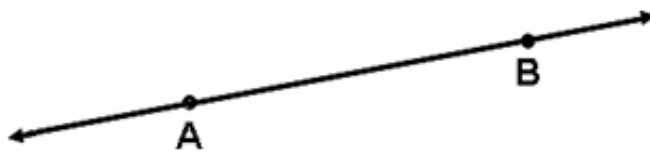


annaclassesonline.com

Lines and Angles

Introduction to line and the terms related to it

- A **line** is a breadthless length which has no end point. Here, AB is a line and it is denoted by $\overleftrightarrow{AB}$.



- A **line segment** is a part of a line which has two end points. Here, AB is a line segment and it is denoted by $\overline{AB}$.



- A **ray** is a part of a line which has only one end point. Here, AB is a ray and it is denoted by $\overrightarrow{AB}$.

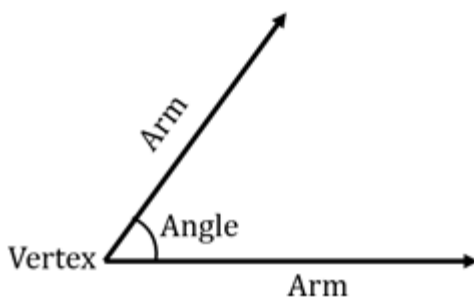


Collinear/Non-collinear points

- Three or more points which lie on the same line are called **collinear points**.
- Three or more points which do not lie on a straight line are called **non-collinear points**.

Introduction to Angle

- An **angle** is formed when two rays originate from the same end point.
- The rays making an angle are called the **arms** of the angle.
- The end point from where the two rays originate to form an angle is called the **vertex** of the angle.



Types of angles:



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



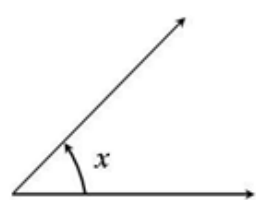
8920488990



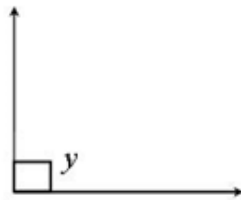
annaclasses.btb@gmail.com



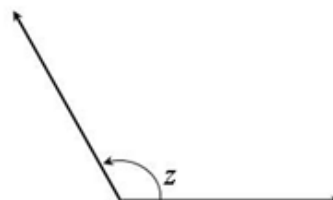
annaclassesonline.com



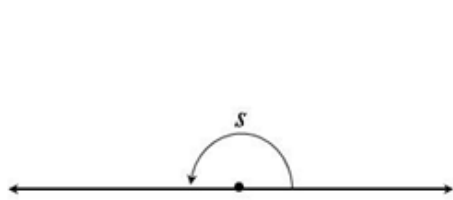
(i) Acute angle: $0^\circ < x < 90^\circ$



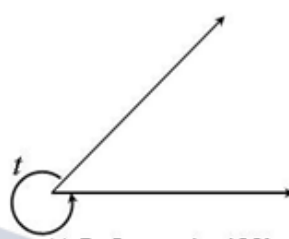
(ii) Right angle: $y = 90^\circ$



(iii) Obtuse angle: $90^\circ < z < 180^\circ$



(iv) Straight angle: $s = 180^\circ$

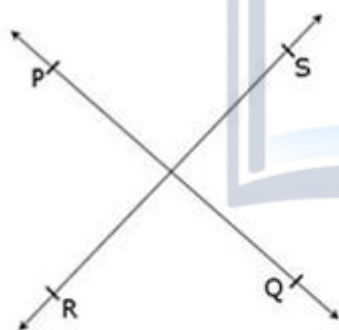


(v) Reflex angle: $180^\circ < t < 360^\circ$

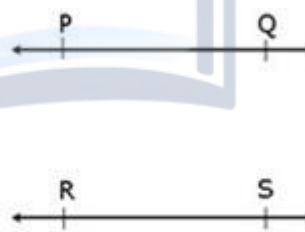
Pair of Angles

- Two angles whose sum is 90° are called **complementary angles**.
- Two angles whose sum is 180° are called **supplementary angles**.

Intersecting and non-intersecting lines



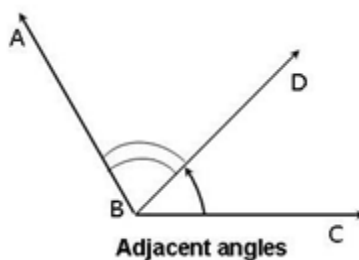
(i) Intersecting lines



(ii) Non-intersecting (parallel) lines

Adjacent angles

Two angles are **adjacent**, if they have a common vertex, a common arm and their non-common arms are on different sides of the common arm.



In the figure, $\angle ABD$ and $\angle DBC$ are adjacent angles.

Linear pair of angles



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



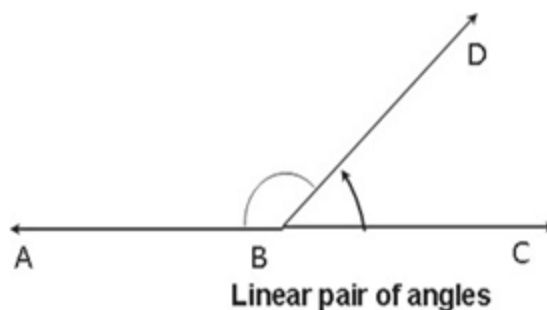
annaclasses.btb@gmail.com



annaclassesonline.com

If a ray stands on a line, then the sum of the two adjacent angles so formed is 180° and vice-versa. This property is called as the **linear pair axiom** and the angles are called **linear pair of angles**.

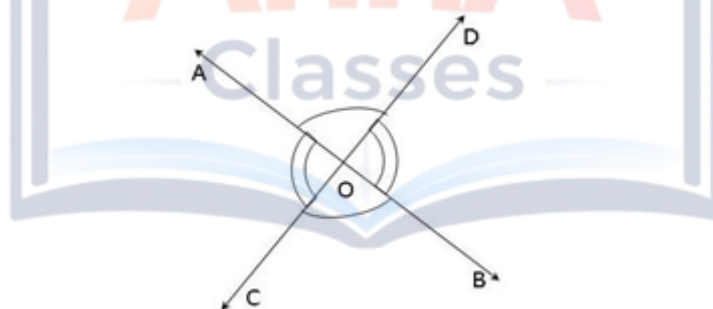
In the figure, $\angle ABD$ and $\angle DBC$ are linear pair of angles i.e. $\angle ABD + \angle DBC = 180^\circ$.



If the sum of two adjacent angles is 180° , then the non-common arms of the angles form a line.

Vertically opposite angles

- The **vertically opposite angles** formed when two lines intersect each other.
- There are two pairs of vertically opposite angles in the given figure and they are $\angle AOD$ and $\angle BOC$, $\angle AOC$ and $\angle BOD$.

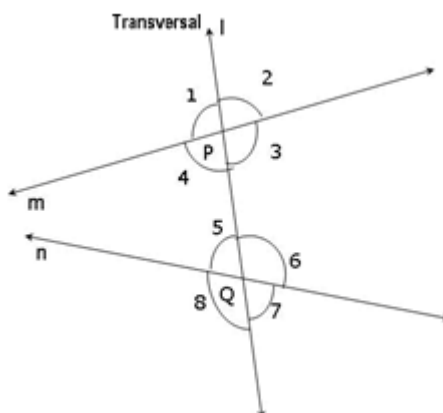


If two lines intersect each other, then the **vertically opposite angles** are equal.

Transversal

A line which intersects two or more lines at distinct points is called a **transversal**.

Pair of angles when a transversal intersects two lines



- **Corresponding angles:**



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6–12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

a) $\angle 1$ and $\angle 5$

b) $\angle 2$ and $\angle 6$

c) $\angle 4$ and $\angle 8$

d) $\angle 3$ and $\angle 7$

- **Alternate interior angles:**

a) $\angle 4$ and $\angle 6$

b) $\angle 3$ and $\angle 5$

- **Alternate exterior angles:**

a) $\angle 1$ and $\angle 7$

b) $\angle 2$ and $\angle 8$

- Interior angles on the same side of the transversal are referred as co-interior angles/ allied angles/ consecutive interior angles and they are:

a) $\angle 4$ and $\angle 5$

b) $\angle 3$ and $\angle 6$

If a transversal intersects two parallel lines, then

- Each pair of **corresponding angles** are equal.
- Each pair of **alternate interior angles** are equal.
- Each pair of interior angles on the same side of the transversal are supplementary.

If a transversal intersects two lines

- Such that a pair of **corresponding angles** is equal, then the two **lines are parallel**.
- Such that a pair of **alternate interior angles** is equal, then the two **lines are parallel**.
- Such that a pair of **interior angles** on the same side of the transversal is supplementary, then the two **lines are parallel**.
- Such that the bisectors of a pair of **corresponding angles** are parallel, then the two **lines are parallel**.

Lines parallel to the same line

Two lines which are parallel to the same line are parallel to each other. This holds for more than two lines also i.e. if two or more lines are parallel to the same line then they will be parallel to each other.

Angle sum property of a triangle

- The sum of the angles of a triangle is 180° . This is known as the **angle sum property of a triangle**.



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



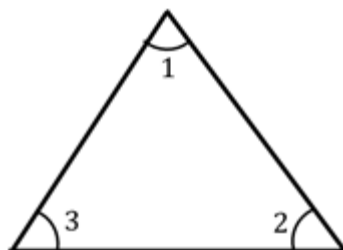
8920488990



annaclasses.btb@gmail.com

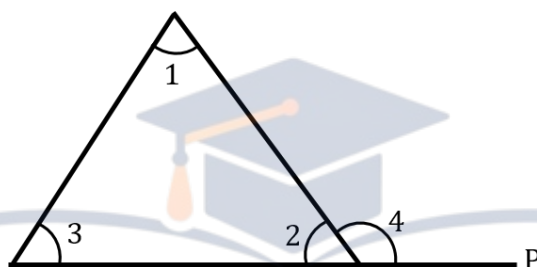


annaclassesonline.com



Here, $\angle 1 + \angle 2 + \angle 3 = 180^\circ$.

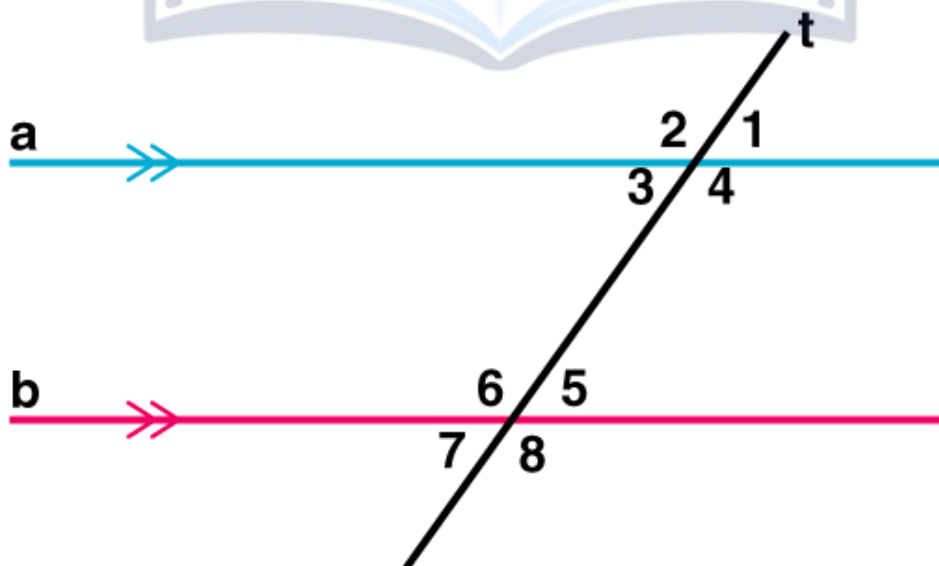
- If a side of a triangle is produced, then the exterior angle so formed is equal to the sum of the two interior opposite angles. This is known as the **exterior angle property of a triangle**.



Here, $\angle 4 = \angle 1 + \angle 3$.

- An exterior angle of a triangle is greater than either of its interior opposite angles. In the above figure, $\angle 4 > \angle 1$ and $\angle 4 > \angle 3$.

Parallel lines with a transversal



- $\angle 1 = \angle 5$, $\angle 2 = \angle 6$, $\angle 4 = \angle 8$ and $\angle 3 = \angle 7$ (Corresponding angles)
- $\angle 3 = \angle 5$, $\angle 4 = \angle 6$ (Alternate interior angles)
- $\angle 1 = \angle 7$, $\angle 2 = \angle 8$ (Alternate exterior angles)

Angles and types of angles

When 2 rays originate from the same point at different directions, they form an angle.



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

The rays are called arms and the common point is called the vertex

Types of angles:

- Acute angle $0^\circ < a < 90^\circ$
- Right angle $a = 90^\circ$
- Obtuse angle: $90^\circ < a < 180^\circ$
- Straight angle $= 180^\circ$
- Reflex Angle $180^\circ < a < 360^\circ$
- Angles that add up to 90° are complementary angles
- Angles that add up to 180° are called supplementary angles.

Intersecting Lines and Associated Angles

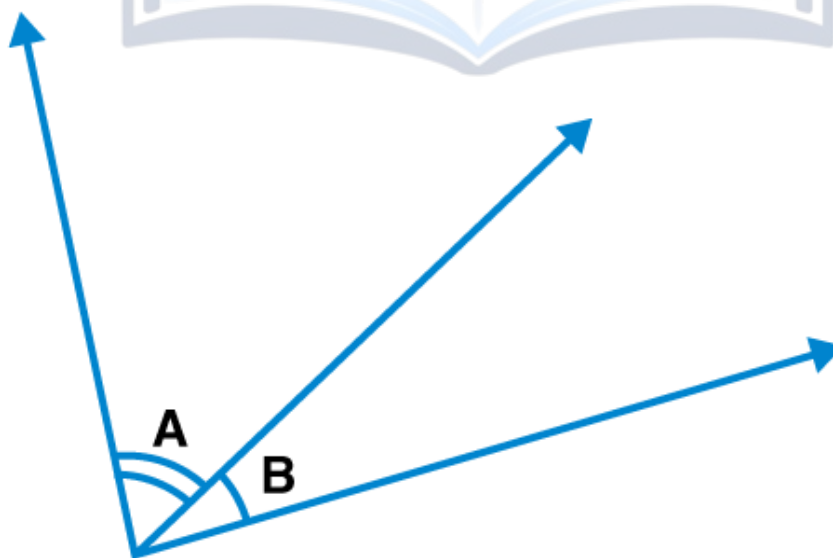
Intersecting and Non-Intersecting lines

When 2 lines meet at a point they are called intersecting

When 2 lines never meet at a point, they are called non-intersecting or parallel lines

Adjacent angles

2 angles are adjacent if they have the same vertex and one common point.



Linear Pair

When 2 adjacent angles are supplementary, i.e they form a straight line (add up to 180°), they are called a linear pair.

Vertically opposite angles

When two lines intersect at a point, they form equal angles that are vertically opposite to each other.



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

Basic Properties of a Triangle

All the properties of a triangle are based on its sides and angles. By the definition of triangle, we know that it is a closed polygon that consists of three sides and three vertices. Also, the sum of all three internal angles of a triangle equal to 180° .

Depending upon the length of sides and measure of angles, the triangles are classified into different types of triangles.

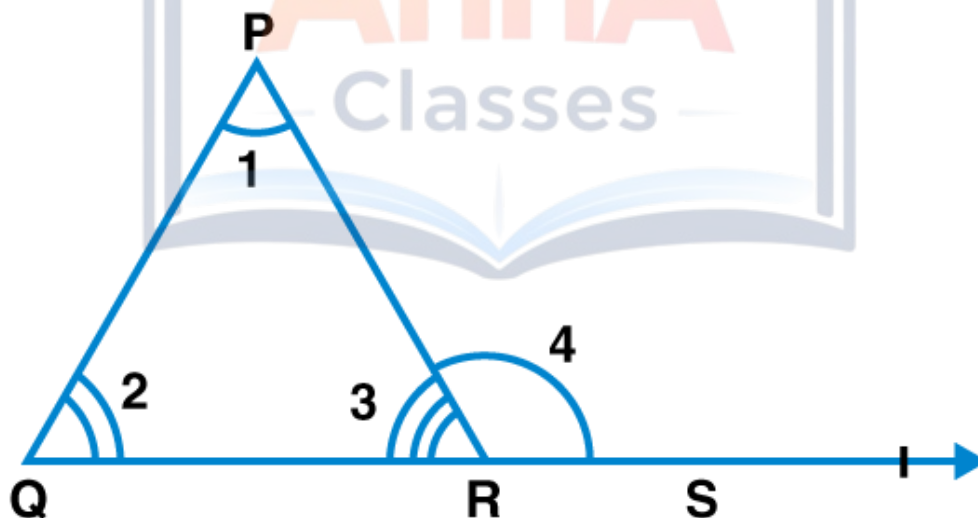
In the beginning, we start from understanding the shape of triangles, its types and properties, theorems based on it such as Pythagoras theorem, etc. In higher classes, we deal with trigonometry, where the right-angled triangle is the base of the concept. Let us learn here some of the fundamentals of the triangle by knowing its properties.

Triangle and sum of its internal angles

Sum of all angles of a triangle add up to 180°

An exterior angle of a triangle = sum of opposite internal angles

– If a side of a triangle is produced, then the exterior angle so formed is equal to the sum of the two interior opposite angles



$$- \angle 4 = \angle 1 + \angle 2$$

Types of Triangle

Based on the Sides	Based on the Angles
Scalene Triangle	Acute angled Triangle
Isosceles Triangle	Right angle Triangle
Equilateral Triangle	Obtuse-angled Triangle



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

So before, discussing the properties of triangles, let us discuss types of triangles given above.

Scalene Triangle: All the sides and angles are unequal.

Isosceles Triangle: It has two equal sides. Also, the angles opposite these equal sides are equal.

Equilateral Triangle: All the sides are equal and all the three angles equal to 60° .

Acute Angled Triangle: A triangle having all its angles less than 90° .

Right Angled Triangle: A triangle having one of the three angles exactly 90° .

Obtuse Angled Triangle: A triangle having one of the three angles more than 90° .

Triangle Formula

- Area of a triangle is the region occupied by a triangle in a two-dimensional plane. The dimension of the area is square units. The formula for area is given by;

$$\text{Area} = \frac{1}{2} \times \text{Base} \times \text{Height}$$

- The perimeter of a triangle is the length of the outer boundary of a triangle. To find the perimeter of a triangle we need to add the length of the sides of the triangle.

$$P = a + b + c$$

- Semi-perimeter of a triangle is half of the perimeter of the triangle. It is represented by s .

$$s = (a + b + c)/2$$

where a , b and c are the sides of the triangle.

- By Heron's formula, the area of the triangle is given by:

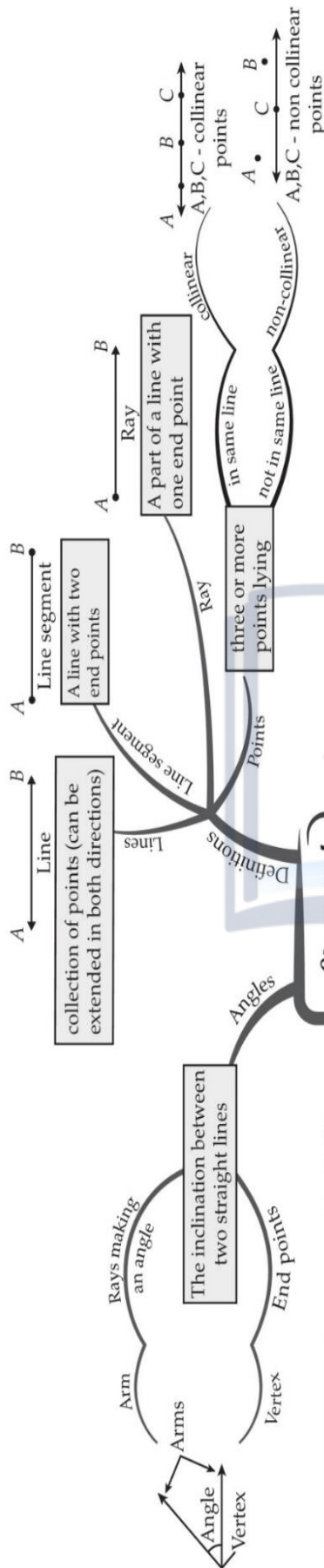
$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

where ' s ' is the semi-perimeter of the triangle.

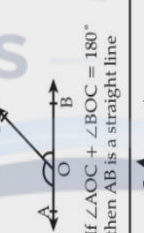
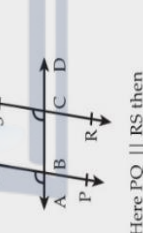
- By the Pythagorean theorem, the hypotenuse of a right-angled triangle can be calculated by the formula:

$$\text{Hypotenuse}^2 = \text{Base}^2 + \text{Perpendicular}^2$$

CHAPTER : 6 LINES AND ANGLES



Angles	Value
Acute	$0^\circ < x < 90^\circ$
Right	$x = 90^\circ$
Obtuse	$90^\circ < x < 180^\circ$
Straight line	$x = 180^\circ$
Reflex	$180^\circ < x < 360^\circ$

1. If a ray stands on a line, then the sum of two adjacent angles so formed is 180°	
2. If the sum of two adjacent angles is 180° , then the non-common arms of the angles form a line.	
3. If a transversal intersects two parallel lines, then each pair of corresponding angles is equal.	
4. If a transversal intersects two lines such that a pair of corresponding angles is equal, then the two lines are parallel to each other.	



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

Important Questions

Multiple Choice Questions-

Question 1. In a right-angled triangle where angle $A = 90^\circ$ and $AB = AC$. What are the values of angle B ?

- (a) 45°
- (b) 35°
- (c) 75°
- (d) 65°

Question 2. In a triangle ABC if $\angle A = 53^\circ$ and $\angle C = 44^\circ$ then the value of $\angle B$ is:

- (a) 46°
- (b) 83°
- (c) 93°
- (d) 73°

Question 3. Given four points such that no three of them are collinear, then the number of lines that can be drawn through them are:

- (a) 4 lines
- (b) 8 lines
- (c) 6 lines
- (d) 2 lines

Question 4. If one angle of triangle is equal to the sum of the other two angles then triangle is:

- (a) Acute triangle
- (b) Obtuse triangle
- (c) Right triangle
- (d) None of these

Question 5. How many degrees are there in an angle which equals one-fifth of its supplement?

- (a) 15°
- (b) 30°
- (c) 75°
- (d) 150°

Question 6. Sum of the measure of an angle and its vertically opposite angle is



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

always.

- (a) Zero
- (b) Thrice the measure of the original angle
- (c) Double the measure of the original angle
- (d) Equal to the measure of the original angle

Question 7. If two parallel lines are cut by a transversal, then the pairs of corresponding angles are congruent.

- (a) Equal
- (b) Complementary
- (c) Supplementary
- (d) corresponding

Question 8. The bisectors of the base angles of an isosceles triangle ABC, with $AB = AC$, meet at O. If $\angle B = \angle C = 50^\circ$. What is the measure of angle O?

- (a) 120°
- (b) 130°
- (c) 80°
- (d) 150°

Question 9. The angles of a triangle are in the ratio 2 : 3 : 4. The angles, in order, are :

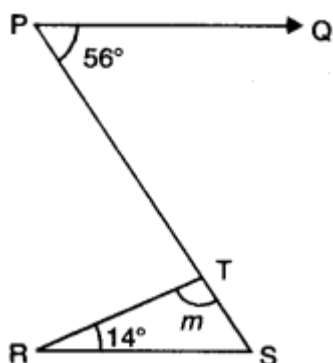
- (a) $80^\circ, 40^\circ, 60^\circ$
- (b) $20^\circ, 60^\circ, 80^\circ$
- (c) $40^\circ, 60^\circ, 80^\circ$
- (d) $60^\circ, 40^\circ, 80^\circ$

Question 10. An acute angle is:

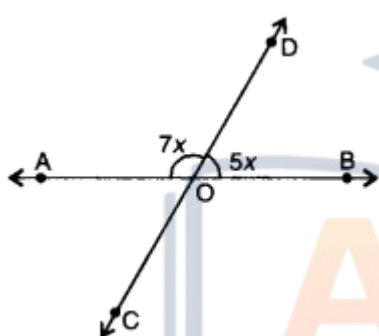
- (a) More than 90 degrees
- (b) Less than 90 degrees
- (c) Equal to 90 degrees
- (d) Equal to 180 degrees

Very Short:

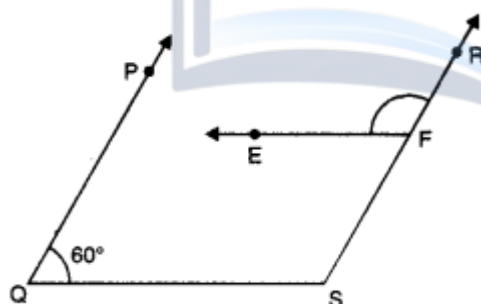
1. If an angle is half of its complementary angle, then find its degree measure.
2. The two complementary angles are in the ratio 1 : 5. Find the measures of the angles.
3. In the given figure, if $PQ \parallel RS$, then find the measure of angle m.



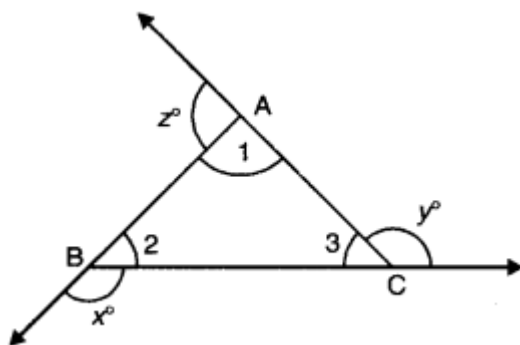
4. If an angle is 140 more than its complement, then find its measure.
5. If $AB \parallel EF$ and $EF \parallel CD$, then find the value of x .
6. In the given figure, lines AB and CD intersect at O . Find the value of x .



7. In the given figure, $PQ \parallel RS$ and $EF \parallel QS$. If $\angle PQS = 60^\circ$, then find the measure of $\angle RFE$.



8. In the given figure, if x° , y° and z° are exterior angles of $\triangle ABC$, then find the value of $x^\circ + y^\circ + z^\circ$.



Short Questions:

1. In the given figure, $AB \parallel CD$, $\angle FAE = 90^\circ$, $\angle AFE = 40^\circ$, find $\angle ECD$.



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



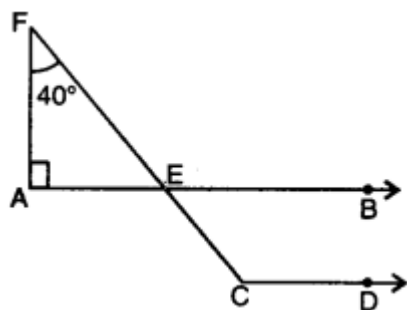
8920488990



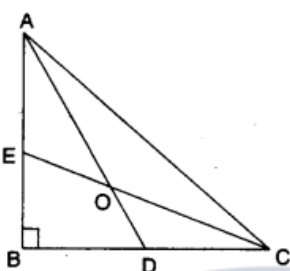
annaclasses.btb@gmail.com



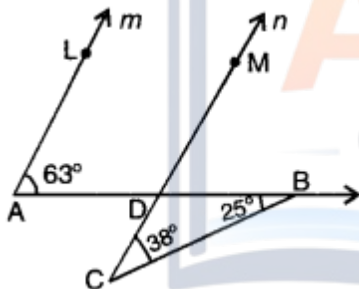
annaclassesonline.com



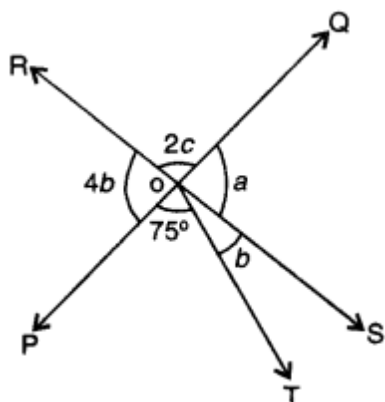
2. In the fig., AD and CE are the angle bisectors of $\angle A$ and $\angle C$ respectively. If $\angle ABC = 90^\circ$, then find $\angle AOC$.



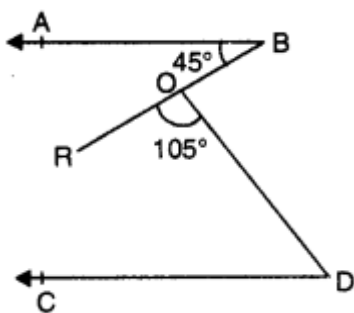
3. In the given figure, prove that $m \parallel n$.



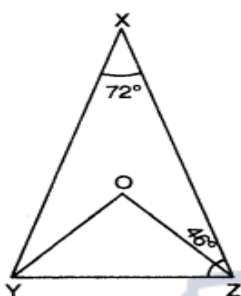
4. In the given figure, two straight lines PQ and RS intersect each other at O. If $\angle POT = 75^\circ$, find the values of a , b , c .



5. In figure, if $AB \parallel CD$. If $\angle ABR = 45^\circ$ and $\angle ROD = 105^\circ$, then find $\angle ODC$.

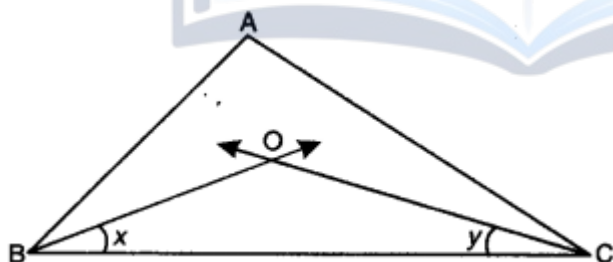


6. In the figure, $\angle X = 72^\circ$, $\angle XZY = 46^\circ$. If YO and ZO are bisectors of $\angle XYZ$ and $\angle XZY$ respectively of $\triangle XYZ$, find $\angle OYZ$ and $\angle YOZ$.

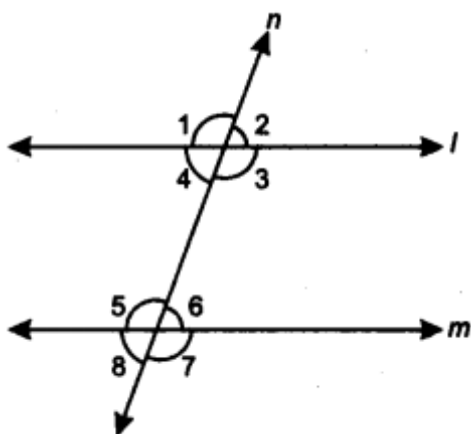


Long Questions:

1. If two parallel lines are intersected by a transversal, prove that the bisectors of two pairs of interior angles form a rectangle.
2. If in $\triangle ABC$, the bisectors of $\angle B$ and $\angle C$ intersect each other at O. Prove that $\angle BOC = 90^\circ + \frac{1}{2} \angle A$



3. In figure, if $l \parallel m$ and $\angle 1 = (2x + y)^\circ$, $\angle 4 = (x + 2y)^\circ$ and $\angle 6 = (3y + 20)^\circ$. Find $\angle 7$ and $\angle 8$.



4. In the given figure, if $PQ \perp PS$, $PQ \parallel SR$, $\angle SQR = 28^\circ$ and $\angle QRT = 65^\circ$. Find the values of x , y and z .



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



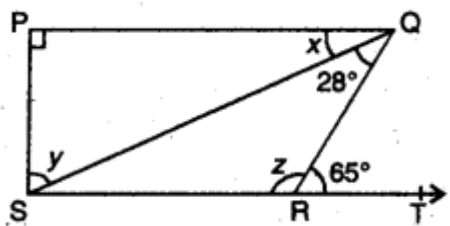
8920488990



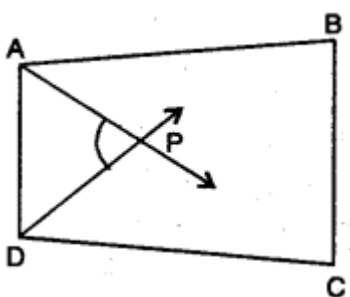
annaclasses.btb@gmail.com



annaclassesonline.com



5. In figure, AP and DP are bisectors of two adjacent angles A and D of a quadrilateral ABCD. Prove that $2\angle APD = \angle B + \angle C$.



Assertion and Reason Questions-

1. In these questions, a statement of assertion followed by a statement of reason is given. Choose the correct answer out of the following choices.

- Assertion and reason both are correct statements and reason is correct explanation for assertion.
- Assertion and reason both are correct statements but reason is not correct explanation for assertion.
- Assertion is correct statement but reason is wrong statement.
- Assertion is wrong statement but reason is correct statement.

Assertion: Two adjacent angles always form a linear pair..

Reason: In a linear pair of angles two non-common arms are opposite rays.

2. In these questions, a statement of assertion followed by a statement of reason is given. Choose the correct answer out of the following choices.

- Assertion and reason both are correct statements and reason is correct explanation for assertion.
- Assertion and reason both are correct statements but reason is not correct explanation for assertion.
- Assertion is correct statement but reason is wrong statement.
- Assertion is wrong statement but reason is correct statement.

Assertion: A triangle can have two obtuse angles.

Reason: Sum of the three angles in a triangle is always 180° .

Case Study Questions-

1. Read the Source/ Text given below and answer these questions:



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



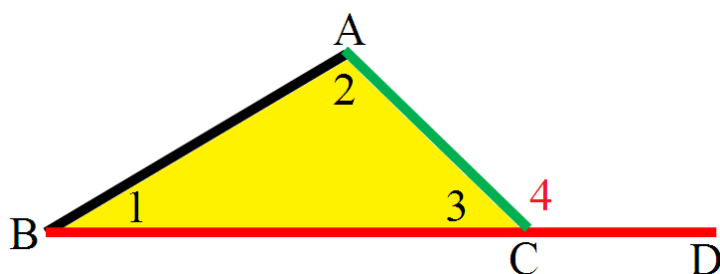
8920488990



annaclasses.btb@gmail.com



annaclassesonline.com



Ashok is studying in 9th class in Govt School, Chhatarpur. Once he was at his home and was doing his geometry homework. He was trying to measure three angles of a triangle using the Dee, but his dee was old and his Dee's numbers were erased and the lines on the dee were visible. Let us help Ashok to find the angles of the triangle. He found that the second angle of the triangle was three times as large as the first. The measure of the third angle is double of the first angle.

Now answer the following questions:

i. What was the value of the first angle?

- a. 30°
- b. 45°
- c. 60°
- d. 90°

ii. What was the value of the third angle?

- a. 30°
- b. 45°
- c. 60°
- d. 90°

iii. What was the value of the second angle?

- a. 30°
- b. 45°
- c. 60°
- d. 90°

iv. What was the value of $\angle 4$ as shown the figure?

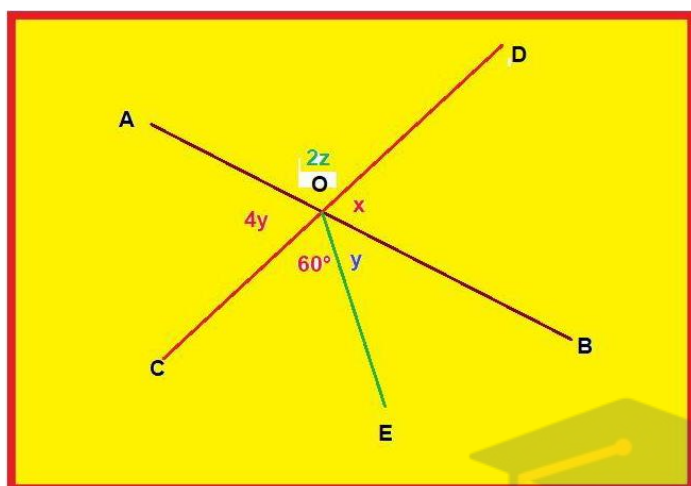
- a. 120°
- b. 45°
- c. 60°
- d. 90°

v. What was the sum of all three angles measured by Ashok using Dee?

- a. 270°
- b. 180°
- c. 100°
- d. 90°

2. Read the Source/ Text given below and answer any four questions:

Maths teacher draws a straight line AB shown on the blackboard as per the following figure.



- Now he told Raju to draw another line CD as in the figure.
- The teacher told Ajay to mark $\angle AOD$ as $2z$.
- Suraj was told to mark $\angle AOC$ as $4y$.
- Clive Made and angle $\angle COE = 60^\circ$.
- Peter marked $\angle BOE$ and $\angle BOD$ as y and x respectively.

Now answer the following questions:

- What is the value of x ?
 - 48°
 - 96°
 - 100°
 - 120°
- What is the value of y ?
 - 48°
 - 96°
 - 100°
 - 24°
- What is the value of z ?
 - 48°
 - 96°
 - 42°
 - 120°
- What should be the value of $x + 2z$?
 - 148°
 - 360°
 - 180°
 - 120°



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

v. What is the relation between y and z ?

- a. $2y + z = 90^\circ$
- b. $2y + z = 180^\circ$
- c. $4y + 2z = 120^\circ$
- d. $y = 2z$

Answer Key:

MCQ:

1. (a) 45°
2. (b) 83°
3. (c) 6 lines
4. (c) Right triangle
5. (b) 30°
6. (c) Double the measure of the original angle
7. (d) Corresponding
8. (b) 130°
9. (c) $40^\circ, 60^\circ, 80^\circ$
10. (b) Less than 90 degrees

Very Short Answer:

1. Let the required angle be x

$$\therefore \text{Its complement} = 90^\circ - x$$

Now, according to given statement, we obtain

$$x = \frac{1}{2}(90^\circ - x)$$

$$\Rightarrow 2x = 90^\circ - x$$

$$\Rightarrow 3x = 90^\circ$$

$$\Rightarrow x = 30^\circ$$

Hence, the required angle is 30° .

2. Let the two complementary angles be x and $5x$.

$$\therefore x + 5x = 90^\circ$$

$$\Rightarrow 6x = 90^\circ$$

$$\Rightarrow x = 15^\circ$$

3. Here, $PQ \parallel RS$, PS is a transversal.

$$\Rightarrow \angle PSR = \angle SPQ = 56^\circ$$

$$\text{Also, } \angle TRS + m + \angle TSR = 180^\circ$$



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

$$14^\circ + m + 56^\circ = 180^\circ$$

$$\Rightarrow m = 180^\circ - 14 - 56 = 110^\circ$$

4. Let the required angle be x

$$\therefore \text{Its complement} = 90^\circ - x$$

Now, according to given statement, we obtain

$$x = 90^\circ - x + 14^\circ$$

$$\Rightarrow 2x = 104^\circ$$

$$\Rightarrow x = 52^\circ$$

Hence, the required angle is 52° .

5. Since $EF \parallel CD \therefore y + 150^\circ = 180^\circ$

$$\Rightarrow y = 180^\circ - 150^\circ = 30^\circ$$

Now, $\angle BCD = \angle ABC$

$$x + y = 70^\circ$$

$$x + 30 = 70$$

$$\Rightarrow x = 70^\circ - 30^\circ = 40^\circ$$

Hence, the value of x is 40°

6. Here, lines AB and CD intersect at O .

$\therefore \angle AOD$ and $\angle BOD$ forming a linear pair

$$\Rightarrow \angle AOD + \angle BOD = 180^\circ$$

$$\Rightarrow 7x + 5x = 180^\circ$$

$$\Rightarrow 12x = 180^\circ$$

$$\Rightarrow x = 15^\circ$$

7. Since $PQ \parallel RS$

$$\therefore \angle PQS + \angle QSR = 180^\circ$$

$$\Rightarrow 60^\circ + \angle QSR = 180^\circ$$

$$\Rightarrow \angle QSR = 120^\circ$$

Now, $EF \parallel QS$

$$\Rightarrow \angle RFE = \angle QSR \text{ [corresponding } \angle\text{s]}$$

$$\Rightarrow \angle RFE = 120^\circ$$

8. We know that an exterior angle of a triangle is equal to sum of two opposite interior angles.

$$\Rightarrow x^\circ = \angle 1 + \angle 3$$

$$\Rightarrow y^\circ = \angle 2 + \angle 1$$



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

$$\Rightarrow z^\circ = \angle 3 + \angle 2$$

Adding all these, we have

$$x^\circ + y^\circ + z^\circ = 2(\angle 1 + \angle 2 + \angle 3)$$

$$= 2 \times 180^\circ$$

$$= 360^\circ$$

Short Answer:

Ans: 1. In AFAE,

$$\text{ext. } \angle FEB = \angle A + \angle F$$

$$= 90^\circ + 40^\circ = 130^\circ$$

Since $AB \parallel CD$

$$\therefore \angle ECD = \angle FEB = 130^\circ$$

Hence, $\angle ECD = 130^\circ$.

Ans: 2. $\because$ AD and CE are the bisector of $\angle A$ and $\angle C$

$$\therefore \angle OAC = \frac{1}{2} \angle A \text{ and}$$

$$\angle OCA = \frac{1}{2} \angle C$$

$$\begin{aligned} \Rightarrow \angle OAC + \angle OCA &= \frac{1}{2} (\angle A + \angle C) \\ &= \frac{1}{2} (180^\circ - \angle B) \quad [\because \angle A + \angle B + \angle C = 180^\circ] \\ &= \frac{1}{2} (180^\circ - 90^\circ) \quad [\because \angle ABC = 90^\circ] \\ &= \frac{1}{2} \times 90^\circ = 45^\circ \end{aligned}$$

In $\triangle AOC$,

$$\angle AOC + \angle OAC + \angle OCA = 180^\circ$$

$$\Rightarrow \angle AOC + 45^\circ = 180^\circ$$

$$\Rightarrow \angle AOC = 180^\circ - 45^\circ = 135^\circ$$

Ans: 3. In $\triangle BCD$,

$$\text{ext. } \angle BDM = \angle C + \angle B$$

$$= 38^\circ + 25^\circ = 63^\circ$$

Now, $\angle LAD = \angle MDB = 63^\circ$

But these are corresponding angles.



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

Hence, $m \parallel n$

Ans: 4. Here, $4b + 75^\circ + b = 180^\circ$ [a straight angle]

$$5b = 180^\circ - 75^\circ = 105^\circ$$

$$b = \frac{105^\circ}{5} = 21^\circ$$

$$\therefore a = 4b = 4 \times 21^\circ = 84^\circ \text{ (vertically opp. } \angle\text{s)}$$

Again, $2c + a = 180^\circ$ [a linear pair]

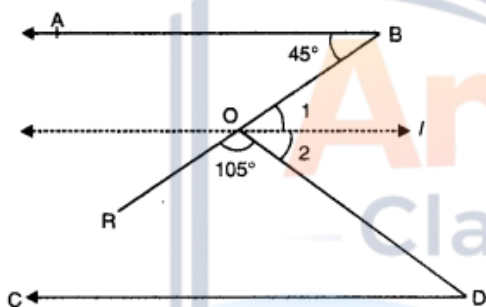
$$\Rightarrow 2c + 84^\circ = 180^\circ$$

$$\Rightarrow 2c = 96^\circ$$

$$\Rightarrow c = \frac{96^\circ}{2} = 48^\circ$$

Hence, the values of a , b and c are $a = 84^\circ$, $b = 21^\circ$ and $c = 48^\circ$.

Ans: 5.



Through O, draw a line 'l' parallel to AB.

$\Rightarrow$ line l will also parallel to CD, then

$$\angle 1 = 45^\circ \text{ [alternate int. angles]}$$

$$\angle 1 + \angle 2 + 105^\circ = 180^\circ \text{ [straight angle]}$$

$$\angle 2 = 180^\circ - 105^\circ - 45^\circ$$

$$\Rightarrow \angle 2 = 30^\circ$$

Now, $\angle ODC = \angle 2$ [alternate int. angles]

$$= \angle ODC = 30^\circ$$

Ans: 6. In $\triangle XYZ$, we have

$$\angle X + \angle Y + \angle Z = 180^\circ$$

$$\Rightarrow \angle Y + \angle Z = 180^\circ - \angle X$$

$$\Rightarrow \angle Y + \angle Z = 180^\circ - 72^\circ$$

$$\Rightarrow \angle Y + \angle Z = 108^\circ$$

$$\Rightarrow \frac{1}{2} \angle Y + \frac{1}{2} \angle Z = \frac{1}{2} \times 108^\circ$$

$$\angle OYZ + \angle OZY = 54^\circ$$



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

[$\because$ YO and ZO are the bisector of $\angle XYZ$ and $\angle XZY$]

$$\Rightarrow \angle OYZ + \frac{1}{2} \times 46^\circ = 54^\circ$$

$$\angle OYZ + 23^\circ = 54^\circ$$

$$\Rightarrow \angle OYZ = 54^\circ - 23^\circ = 31^\circ$$

In $\triangle YOZ$, we have

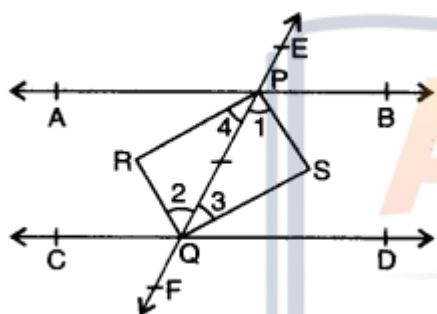
$$\angle YOZ = 180^\circ - (\angle OYZ + \angle OZY)$$

$$= 180^\circ - (31^\circ + 23^\circ) = 180^\circ - 54^\circ = 126^\circ$$

Long Answer:

Ans: 1. Given: $AB \parallel CD$ and transversal EF cut them at P and Q respectively and the bisectors of

pair of interior angles form a quadrilateral $PRQS$



To Prove: $PRQS$ is a rectangle.

Proof: $\because$ PS , QR , QS and PR are the bisectors of angles $\angle BPQ$, $\angle CQP$, $\angle DQP$ and $\angle APQ$ respectively.

$$\therefore \angle 1 = \frac{1}{2} \angle BPQ, \angle 2 = \frac{1}{2} \angle CQP,$$

$$\angle 3 = \frac{1}{2} \angle DQP \text{ and } \angle 4 = \frac{1}{2} \angle APQ$$

Now, $AB \parallel CD$ and EF is a transversal

$$\therefore \angle BPQ = \angle CQP$$

$$\Rightarrow \angle 1 = \angle 2 \left(\because \angle 1 = \frac{1}{2} \angle BPQ \text{ and } \angle 2 = \frac{1}{2} \angle CQP \right)$$

But these are pairs of alternate interior angles of PS and QR

$$\therefore PS \parallel QR$$

Similarly, we can prove $\angle 3 = \angle 4 \Rightarrow QS \parallel PR$

$\therefore PRQS$ is a parallelogram.

$$\text{Further } \angle 1 + \angle 3 = \frac{1}{2} \angle BPQ + \frac{1}{2} \angle DQP = \frac{1}{2} (\angle BPQ + \angle DQP)$$

$$= \frac{1}{2} \times 180^\circ = 90^\circ \left(\because \angle BPQ + \angle DQP = 180^\circ \right)$$

$$\therefore \text{In } \triangle PSQ, \text{ we have } \angle PSQ = 180^\circ - (\angle 1 + \angle 3) = 180^\circ - 90^\circ = 90^\circ$$

Thus, $PRQS$ is a parallelogram whose one angle $\angle PSQ = 90^\circ$.



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

Hence, PRQS is a rectangle.

Ans: 2. Let $\angle B = 2x$ and $\angle C = 2y$

$\therefore$ OB and OC bisect $\angle B$ and $\angle C$ respectively.

$$\angle OBC = \frac{1}{2} \angle B = \frac{1}{2} \times 2x = x$$

$$\text{and } \angle OCB = \frac{1}{2} \angle C = \frac{1}{2} \times 2y = y$$

Now, in $\triangle BOC$, we have

$$\angle BOC + \angle OBC + \angle OCB = 180^\circ$$

$$\Rightarrow \angle BOC + x + y = 180^\circ$$

$$\Rightarrow \angle BOC = 180^\circ - (x + y)$$

Now, in $\triangle ABC$, we have

$$\angle A + 2B + C = 180^\circ$$

$$\Rightarrow \angle A + 2x + 2y = 180^\circ$$

$$\Rightarrow 2(x + y) = \frac{1}{2}(180^\circ - \angle A)$$

$$\Rightarrow x + y = 90^\circ - \frac{1}{2} \angle A \dots (ii)$$

From (i) and (ii), we have

$$\angle BOC = 180^\circ - (90^\circ - \frac{1}{2} \angle A) = 90^\circ + \frac{1}{2} \angle A$$

Ans: 3. Here, $\angle 1$ and $\angle 4$ are forming a linear pair

$$\angle 1 + \angle 4 = 180^\circ$$

$$(2x + y)^\circ + (x + 2y)^\circ = 180^\circ$$

$$3(x + y)^\circ = 180^\circ$$

$$x + y = 60$$

Since $l \parallel m$ and n is a transversal

$$\angle 4 = \angle 6$$

$$(x + 2y)^\circ = (3y + 20)^\circ$$

$$x - y = 20$$

Adding (i) and (ii), we have

$$2x = 80 \Rightarrow x = 40$$

From (i), we have

$$40 + y = 60 \Rightarrow y = 20$$

$$\text{Now, } \angle 1 = (2 \times 40 + 20)^\circ = 100^\circ$$

$$\angle 4 = (40 + 2 \times 20)^\circ = 80^\circ$$

$$\angle 8 = \angle 4 = 80^\circ \text{ [corresponding } \angle \text{s]}$$



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

$$\angle 1 = \angle 3 = 100^\circ \text{ [vertically opp. } \angle\text{s]}$$

$$\angle 7 = \angle 3 = 100^\circ \text{ [corresponding } \angle\text{s]}$$

$$\text{Hence, } \angle 7 = 100^\circ \text{ and } \angle 8 = 80^\circ$$

Ans: 4. Here, $PQ \parallel SR$.

$$\Rightarrow \angle PQR = \angle QRT$$

$$\Rightarrow x + 28^\circ = 65^\circ$$

$$\Rightarrow x = 65^\circ - 28^\circ = 37^\circ$$

$$\text{Now, in it. } \triangle SPQ, \angle P = 90^\circ$$

$$\therefore \angle P + x + y = 180^\circ \text{ [angle sum property]}$$

$$\therefore 90^\circ + 37^\circ + y = 180^\circ$$

$$\Rightarrow y = 180^\circ - 90^\circ - 37^\circ = 53^\circ$$

$$\text{Now, } \angle SRQ + \angle QRT = 180^\circ \text{ [linear pair]}$$

$$z + 65^\circ = 180^\circ$$

$$z = 180^\circ - 65^\circ = 115^\circ$$

Ans: 5. In quadrilateral ABCD, we have

$$\angle A + \angle B + \angle C + \angle D = 360^\circ$$

$$\Rightarrow \frac{1}{2} \angle A + \frac{1}{2} \angle B + \frac{1}{2} \angle C + \frac{1}{2} \angle D = \frac{1}{2} \times 360^\circ$$

$$\Rightarrow \frac{1}{2} \angle A + \frac{1}{2} \angle D = 180^\circ - \frac{1}{2} (\angle B + \angle C)$$

As, AP and DP are the bisectors of $\angle A$ and $\angle D$

$$\therefore \angle PAD = \frac{1}{2} \angle A$$

$$\text{and } \angle PDA = \frac{1}{2} \angle D$$

$$\text{Now, } \angle PAD + \angle PDA = 180^\circ - \frac{1}{2} (\angle B + \angle C) \quad \dots(i)$$

In $\triangle APD$, we have

$$\angle APD + \angle PAD + \angle PDA = 180^\circ$$

$$\Rightarrow \angle APD + 180^\circ - \frac{1}{2} (\angle B + \angle C) = 180^\circ \quad \text{[using (i)]}$$

$$\Rightarrow \angle APD = \frac{1}{2} (\angle B + \angle C)$$

$$\Rightarrow 2\angle APD = \angle B + \angle C$$

Assertion and Reason Answers-

1. d) Assertion is wrong statement but reason is correct statement.

Explanation:

Linear pair



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

Adjacent angles with opposite rays as noncommon arms are called the linear pair.

They form a straight angle.

Hence **Reason is True.**

Two adjacent angles form a linear pair if non common arms are opposite rays.

If non common sides are not opposite rays then adjacent angles does not form a linear pair.

Hence Assertion "Two adjacent angles always form a linear pair" is False

For example two adjacent angles which are complementary forms a right angle not a linear pair.

2. d) Assertion is wrong statement but reason is correct statement.

Explanation:

ASSERTION : A triangle can have two obtuse angles.

Obtuse angle are the angles whos measure are between 90° and 180°

If a triangle has two obtuse angles then sum of those two angles will be

between $(90^\circ + 90^\circ)$ and $(180^\circ + 180^\circ)$

= between 180° and 360°

Hence sum of all the angles of triangle would be greater than 180°

But Sum of all the angles of a triangle is 180°

Hence This is not possible

so Assertion is FALSE

REASON : The sum of all the interior angles of a triangle is 180°

TRUE

Case Study Answers-

1.

(i)	(a)	30°
(ii)	(c)	60°
(iii)	(d)	90°
(iv)	(a)	120°
(v)	(b)	180°

2.



AnnA Classes

Learn Smart. Score High.

Concept-Based
Learning

Experienced
Faculty

For Classes
6-12



8920488990



annaclasses.btb@gmail.com



annaclassesonline.com

(i)	(b)	96°
(ii)	(d)	24°
(iii)	(c)	42°
(iv)	(c)	180°
(v)	(a)	$2y + z = 90^\circ$

